$$
\begin{aligned}
& 9) 5 \\
& \text { Composition of } \\
& \text { Transformations }
\end{aligned}
$$

## WHAT IS IT????

When a transformation is applied to a
figure, and then another
transformation is applied to its $\qquad$
the result is called a
of
the $\qquad$

## KeyConcept Glide Reflection

A glide reflection is the composition of a translation followed by a reflection in a line parallel to the translation vector.

## Example

The glide reflection shown is the composition of a translation along $\vec{w}$ followed by a reflection in line $\ell$.


Find a single transformation for a $75^{\circ}$ counterclockwise rotation with center $(2,1)$ followed by a $38^{\circ}$ counterclockwise rotation with center $(2,1)$
$113^{\circ}$ counterclockwise rotation with center $(2,1)$


# Find a single transformation equivalent to a 

 translation with vector <-2, 7> followed by a translation with vector $\langle 9,3>$.Translation with vector <7, 10>


## Practice

Quadrilateral BGTS has vertices $B(-3,4), G(-1,3), T(-1,1)$, and $S(-4,2)$. Graph BGTS and its image after a translation along $\langle 5,0\rangle$ and a reflection in the $x$-axis.

|  | B |  |  | AV |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  | C |  |  |  |  |

## Practice

Quadrilateral RSTU has vertices $R(1,-1), S(4,-2), T(3,-4)$, and $U(1,-3)$. Graph RSTU and its image after a translation along $\langle-4,1\rangle$ and a reflection in the $x$-axis. Which point is located at $(-3,0)$ ?
A. $R^{\prime}$
B. $S^{\prime}$
C. $T$
D. $U^{\prime}$

|  |  |  |  | $\boldsymbol{y} \boldsymbol{y}$ |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  | $T^{\prime}$ |  |  |  |  |  |  |
|  | $U^{\prime}$ |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  | $S^{\prime}$ |  |  |  |  |  |
| $R^{\prime}$ |  |  | $\mathbf{O}$ | $R$ |  |  |  | $\boldsymbol{x}$ |  |
|  |  |  |  |  |  |  |  | $S$ |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | $U$ |  |  |  |  |
|  |  |  |  |  |  |  |  | $T$ |  |

## Definitions

An is a transformation that preserves shape and size.
Translations, reflections and rotations are

## Theorem 9.2 Reflections in Parallel Lines

The composition of two reflections in parallel lines can be described by a translation vector that is

- perpendicular to the two lines, and
- twice the distance between the two lines.

p. 652


## Reflections over two parallel lines equals...



## Reflections over two intersection lines equals



